

# Digital Signatures

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# What is a Digital Signature

Digital = consisting of a string of digits

PARADOXICAL!

Strings of digits can be copied but signatures are not meant to be copied.



# What are Digital Signatures?

- Material that requires verification
  - Usually when the material is being sent to you instead of you sending the material
- Most well known: Software Signing
  - Valid signatures will tell you the maker of some software and can give the user comfort
  - No signature means no information and this can be potentially dangerous
  - Websites with https send a digitally signed certificate before establishing a secure connection
- Signing your name as a signature
  - Where an online form asks for name

# Paper Signatures

## Signature Bank

Used to compare a person's paper signature to itself to make sure it is valid

Trust the source that the signature is correct

## Problems with Paper Signatures:

Easy to obtain and



[http://www.fdpexpert.com/images/bigstock-Contract-with-person-signing-n-26173646\\_-\\_Copy.jpg](http://www.fdpexpert.com/images/bigstock-Contract-with-person-signing-n-26173646_-_Copy.jpg)

# Signing with a Padlock

## Lock and Keys

Owned by one person, both locks and keys

The owner is the ONLY one who can lock the lock

The owner must physically give someone the key to unlock the lock

Anyone with a key can unlock the lock

## Lock IS signature

Generally need

Ex: In a



lock is the signature

<http://www.globalnerdy.com/wordpress/wp-content/uploads/2014/07/unlocked-padlock-with-key.jpg>

third party that would store the keys for the lock

# Signing with a Multiplicative Padlock

*Physical* → *Numerical*

Padlocks and Keys are represented by numbers

Locking and Unlocking are represented by multiplication in clock arithmetic

Message passed is a sequence of a string of numbers

# Multiplicative Padlock Trick

Message = Number

Padlock = Different number

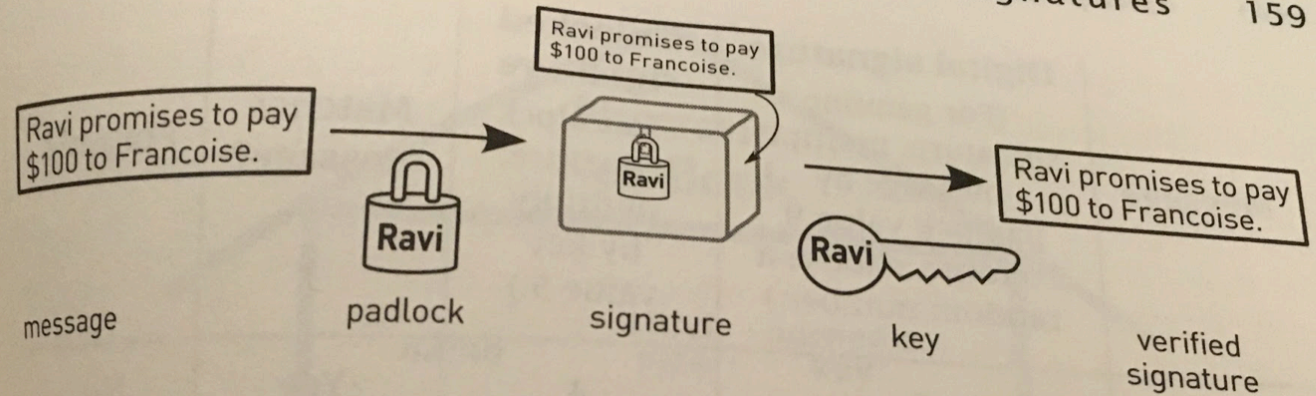
Owner chooses clock size and number to represent the padlock

**Result = Message x Padlock (using multiplication in clock arithmetic)**

Result = Digital signature for original message

Key = number selected to unlock previously chosen padlock number

**Verify Signature = Key x Result (using multiplication in clock arithmetic)**



message	padlock	signature	key	verified signature
5	multiply by 6, with clock size 11	8	multiply by 2, with clock size 11	5
3	multiply by 6, with clock size 11	7	multiply by 2, with clock size 11	3
2	multiply by 6, with clock size 11	1	multiply by 2, with clock size 11	2

How to "lock"



# Padlock Trick cont.

Padlock number MUST be secret

Can reveal message number, signature, key value and clock size

Still need third party

Without third party

the owner can give false key

Others can make padlock and key and say it is the owners

In Short:

**Numeric Padlock : PRIVATE**

# How Numbers are Chosen

Clock size is any prime number

Padlock is any positive number smaller than clock size

Key is generated by a computer using Euclid's algorithm

Flaw: Computer given key value can generate padlock number by applying the algorithm again

Don't use multiplication -- Don't use this approach

# Exponent Padlock

Known as RSA and is the approach used for digital signatures

Same approach as multiplicative technique but using exponentiation

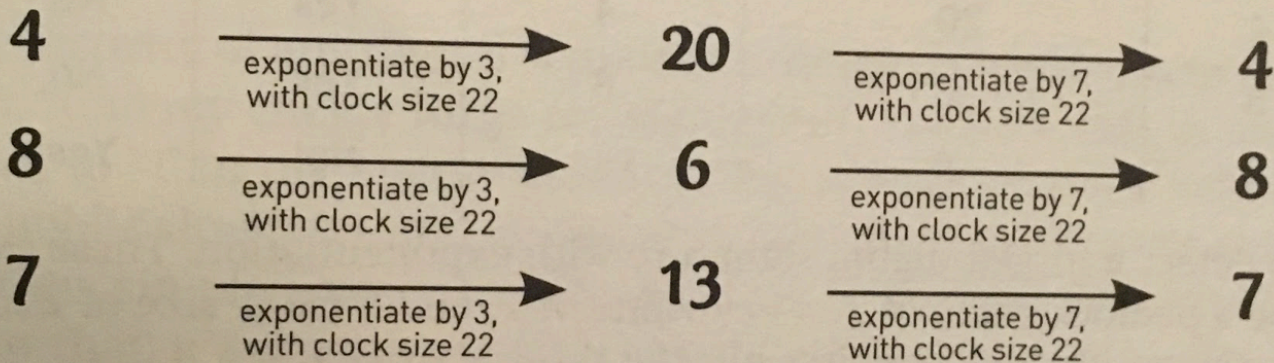
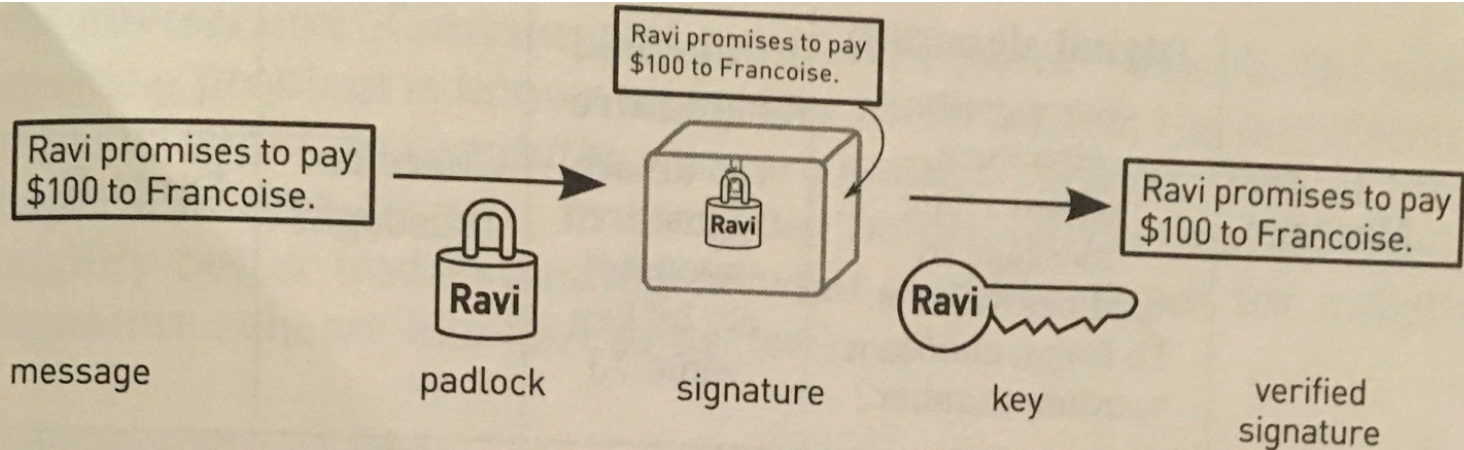
Message = Base

Padlock = Exponent

Signature = result of exponentiation with clock arithmetic

User picks padlock (any number  $<$  clock size) and clock size (any number)

Key is computed by computer



Locking and unlocking messages using exponentiation.

# RSA System

RSA is both Public Key Cryptography Scheme AND Digital Signature Scheme

Person can compute key easily based off of padlock but it is impossible to reverse the process even if you know the clock size

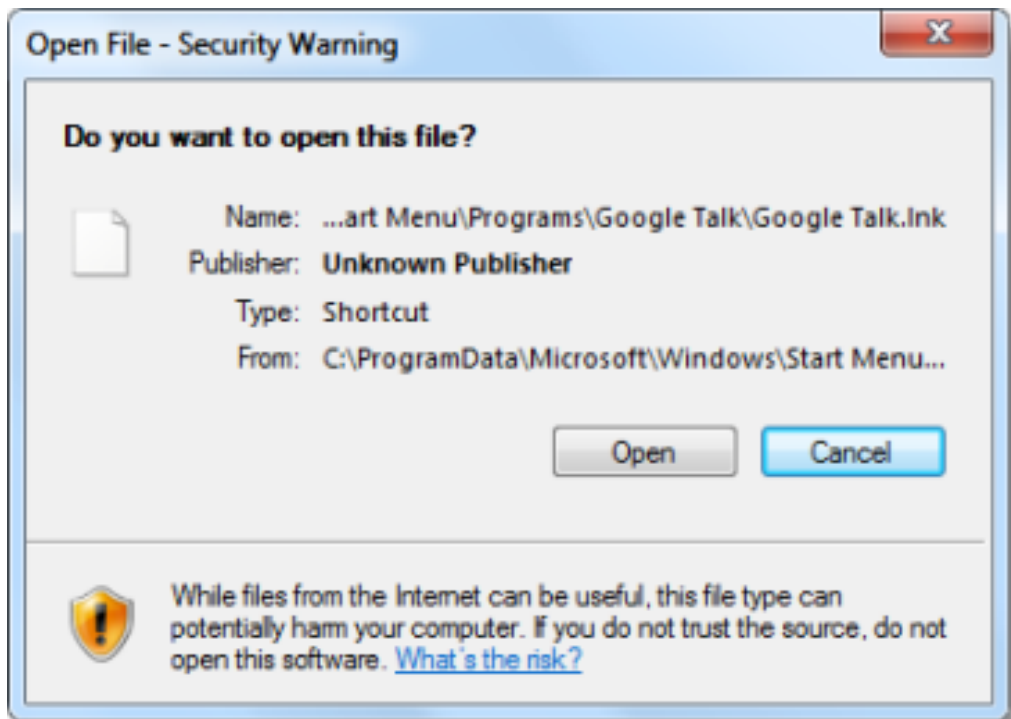
Has not been proven and so the algorithm is considered to be secure for now

To generate clock size for RSA you multiply two prime number together

**Brakes: if clock size is factorized into 2 prime numbers (key can easily be reversed)**

People try to crack it and there is no efficient way even with Quantum computers

# Digital Signatures in Practice



## Certification Authority

Maintain servers that are contacted electronically to download public key information

When the computer gets a signature it comes with information stating which CA can vouch for the signer's public key

CA = THIRD PARTY

How do we trust third party?

<http://www.groovypost.com/wp-content/uploads/2010/10/image36.png>

# Paradox Resolved

What do YOU think?

# Summery

Without digital signatures the internet as we know it would not exist

No sources could be verified

Data could be transferred but not verified